

Algebraic Expressions- Answers

May 2019 Mathematics Advanced Paper 1: Pure Mathematics 1

1.

Question	Scheme	Marks	AOs	
2(i)	$16a^2 = 2\sqrt{a} \Rightarrow a^{\frac{3}{2}} = \frac{1}{8}$	$16a^2 - 2\sqrt{a} = 0$ $\Rightarrow 2a^{\frac{1}{2}}(8a^{\frac{3}{2}} - 1) = 0$ $\Rightarrow a^{\frac{3}{2}} = \frac{1}{8}$	M1	1.1b
	$\Rightarrow a = \left(\frac{1}{8}\right)^{\frac{2}{3}}$	$\Rightarrow a = \left(\frac{1}{8}\right)^{\frac{2}{3}}$	M1	1.1b
	$\Rightarrow a = \frac{1}{4}$	$\Rightarrow a = \frac{1}{4}$	A1	1.1b
	Deduces that $a = 0$ is a solution		B1	2.2a
			(4)	
(ii)	$b^4 + 7b^2 - 18 = 0 \Rightarrow (b^2 + 9)(b^2 - 2) = 0$		M1	1.1b
	$b^2 = -9, 2$		A1	1.1b
	$b^2 = k \Rightarrow b = \sqrt{k}, k > 0$		dM1	2.3
	$b = \sqrt{2}, -\sqrt{2}$ only		A1	1.1b
			(4)	
(8 marks)				

(i)

M1: Combines the two algebraic terms to reach $a^{\pm\frac{3}{2}} = C$ or equivalent such as $(\sqrt{a})^3 = C$
($C \neq 0$)

An alternative is via squaring and combining the algebraic terms to reach $a^{\pm 3} = k, k > 0$

Eg. $\dots a^4 = \dots a \Rightarrow a^{\pm 3} = k$ or $\dots a^4 = \dots a \Rightarrow \dots a^4 - \dots a = 0 \Rightarrow \dots a(a^3 - \dots) = 0 \Rightarrow a^3 = \dots$

Allow for slips on coefficients.

M1: Undoes the indices correctly for their $a^{\frac{m}{n}} = C$ (So M0 M1 A0 is possible)
You may even see logs used.

A1: $a = \frac{1}{4}$ and no other solutions apart from 0 Accept exact equivalents Eg 0.25

B1: Deduces that $a = 0$ is a solution.

(ii)

M1: Attempts to solve as a quadratic equation in b^2

Accept $(b^2 + m)(b^2 + n) = 0$ with $mn = \pm 18$ or solutions via the use of the quadratic

formula Also allow candidates to substitute in another variable, say $u = b^2$ and solve for u

A1: Correct solution. Allow for $b^2 = 2$ or $u = 2$ with no incorrect solution given.

Candidates can choose to omit the solution $b^2 = -9$ or $u = -9$ and so may not be seen

DM1: Finds at least one solution from their $b^2 = k \Rightarrow b = \sqrt{k}, k > 0$. Allow $b = 1.414$

A1: $b = \sqrt{2}$, $-\sqrt{2}$ only. The solution asks for real values so if $3i$ is given then score A0

Answers with minimal or no working:

In part (i)

- no working, just answer(s) with they can score the B1
- If they square and proceed to the quartic equation $256a^4 = 4a$ oe, and then write down the answers they can have access to all marks.

In part (ii)

- Accept for 4 marks $b^2 = 2 \Rightarrow b = \pm\sqrt{2}$
- No working, no marks.

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2.

Question Number	Scheme		Marks
6.(a)	Replaces 2^{2x+1} with $2^{2x} \times 2$ or states $2^{2x+1} = 2^{2x} \times 2$ or states $(2^x)^2 = 2^{2x}$	Uses the addition or power law of indices on 2^{2x} or 2^{2x+1} . E.g. $2^x \times 2^x = 2^{2x}$ or $(2^x)^2 = 2^{2x}$ or $2^{2x+1} = 2 \times 2^{2x}$ or $2^{x+0.5} = 2^x \times \sqrt{2}$ or $2^{2x+1} = (2^{x+0.5})^2$.	M1
	$2^{2x+1} - 17 \times 2^x + 8 = 0$ $\Rightarrow 2y^2 - 17y + 8 = 0^*$	Cso. Complete proof that includes explicit statements for the addition and power law of indices on 2^{2x+1} with no errors. The equation needs to be as printed including the “= 0”. If they work backwards, they do not need to write down the printed answer first but must end with the version in 2^x including ‘= 0’.	A1*

The following are examples of acceptable proofs.		
$2^{2x+1} = (2^{x+0.5})^2 = (2^x \sqrt{2})^2 = (y\sqrt{2})^2 = 2y^2$ $\Rightarrow 2^{2x+1} - 17(2^x) + 8 = 2y^2 - 17y + 8 = 0$		
$2y^2 = 2 \times 2^x \times 2^x = 2^{2x+1}$ $\Rightarrow 2^{2x+1} - 17(2^x) + 8 = 2y^2 - 17y + 8 = 0$		
$2y^2 - 17y + 8 = 0 \Rightarrow 2(2^x)^2 - 17(2^x) + 8 = 0$ $\Rightarrow 2 \times 2^{2x} - 17(2^x) + 8 = 0 \Rightarrow 2^{2x+1} - 17(2^x) + 8 = 0$		
$2^{2x+1} = 2 \times 2^{2x} \Rightarrow 2 \times 2^{2x} - 17(2^x) + 8 = 0$ $\Rightarrow 2y^2 - 17y + 8 = 0$ <p>Scores M1A0 as $2^{2x} = (2^x)^2$ has not been shown explicitly</p>		
<p>Special Case:</p> $2^{2x+1} = 2^1 \times (2^x)^2 \text{ or } 2^{2x+1} = (2^x)^2 \times 2^1$ <p>With or without the multiplication signs and with no subsequent explicit evidence of the power law scores M1A0</p>		
<p>Example of insufficient working:</p> $2^{2x+1} = 2(2^x)^2 = 2y^2$ <p>scores no marks as neither rule has been shown explicitly.</p>		
		(2)

(b)	$2y^2 - 17y + 8 = 0 \Rightarrow (2y-1)(y-8) = 0 \Rightarrow y = \dots$ <p>or</p> $2(2^x)^2 - 17(2^x) + 8 = 0 \Rightarrow (2(2^x) - 1)((2^x) - 8) = 0 \Rightarrow 2^x = \dots$ <p>Solves the given quadratic either in terms of y or in terms of 2^x See General Principles for solving a 3 term quadratic</p> <p>Note that completing the square on e.g. $y^2 - \frac{17}{2}y + 4 = 0$ requires</p> $\left(y \pm \frac{17}{4}\right)^2 \pm q \pm 4 = 0 \Rightarrow y = \dots$		M1
	$(y =) \frac{1}{2}, 8$ or $(2^x =) \frac{1}{2}, 8$	Correct values	A1
	$\Rightarrow 2^x = \frac{1}{2}, 8 \Rightarrow x = -1, 3$	<p>M1: Either finds one correct value of x for their 2^x or obtains a correct numerical expression in terms of logs e.g. for $k > 0$</p> $2^x = k \Rightarrow x = \log_2 k \text{ or } \frac{\log k}{\log 2}$ <p>A1: $x = -1, 3$ only. Must be values of x.</p>	M1 A1
			(4)
		(6 marks)	

3.

Question Number	Scheme	Notes	Marks	
2	9^{3x+1} = for example $3^{2(3x+1)}$ or $(3^2)^{3x+1}$ or $(3^{(3x+1)})^2$ or $3^{3x+1} \times 3^{3x+1}$ or $(3 \times 3)^{3x+1}$ or $3^2 \times (3^2)^{3x}$ or $(9^{\pm})^y$ or $9^{\pm y}$ or $y = 2(3x+1)$	Expresses 9^{3x+1} correctly as a power of 3 or expresses 3^y correctly as a power of 9 or expresses y correctly in terms of x (This mark is not for just $3^2 = 9$)	M1	
	$= 3^{6x+2}$ or $y = 6x + 2$ or $a = 6, b = 2$	Cao (isw if necessary)	A1	
	Providing there is no incorrect work, allow sight of $6x + 2$ to score both marks Correct answer only implies both marks Special case: 3^{6x+1} only scores M1A0			
				[2]
	Alternative using logs			
	$9^{3x+1} = 3^y \Rightarrow \log 9^{3x+1} = \log 3^y$			
	$(3x+1)\log 9 = y \log 3$	Use power law correctly on both sides	M1	
	$y = \frac{\log 9}{\log 3}(3x+1)$			
	$y = 6x + 2$	cao	A1	
				2 marks

4.

Question Number	Scheme	Notes	Marks
3.(a)	$\sqrt{50} - \sqrt{18} = 5\sqrt{2} - 3\sqrt{2}$	$\sqrt{50} = 5\sqrt{2}$ or $\sqrt{18} = 3\sqrt{2}$ and the other term in the form $k\sqrt{2}$. This mark may be implied by the correct answer $2\sqrt{2}$	M1
	$= 2\sqrt{2}$	Or $a = 2$	A1
(b) WAY 1	$\frac{12\sqrt{3}}{\sqrt{50} - \sqrt{18}} = \frac{12\sqrt{3}}{"2"\sqrt{2}}$	Uses part (a) by replacing denominator by their $a\sqrt{2}$ where a is numeric. This is all that is required for this mark.	M1
	$= \frac{12\sqrt{3}}{"2"\sqrt{2}} \times \frac{\sqrt{2}}{\sqrt{2}} = \frac{12\sqrt{6}}{4}$	Rationalises the denominator by a correct method e.g. multiplies numerator and denominator by $k\sqrt{2}$ to obtain a multiple of $\sqrt{6}$. Note that multiplying numerator and denominator by $2\sqrt{2}$ or $-2\sqrt{2}$ is quite common and is acceptable for this mark. May be implied by a correct answer. This is dependent on the first M1.	dM1
	$= 3\sqrt{6}$ or $b = 3, c = 6$	Cao and cso	A1
			[3]

(b) WAY 2	$\frac{12\sqrt{3}}{\sqrt{50}-\sqrt{18}} \times \frac{\sqrt{50}+\sqrt{18}}{\sqrt{50}+\sqrt{18}}$ or $\frac{12\sqrt{3}}{5\sqrt{2}-3\sqrt{2}} \times \frac{5\sqrt{2}+3\sqrt{2}}{5\sqrt{2}+3\sqrt{2}}$	For rationalising the denominator by a correct method i.e. multiplying numerator and denominator by $k(\sqrt{50}+\sqrt{18})$	M1
	$\frac{60\sqrt{6}+36\sqrt{6}}{50-18}$	For replacing numerator by $\alpha\sqrt{6} + \beta\sqrt{6}$. This is dependent on the first M1 and there is no need to consider the denominator for this mark.	dM1
	$= 3\sqrt{6} \text{ or } b=3, c=6$	Cao and cso	A1
			[3]
(b) WAY 3	$\frac{12\sqrt{3}}{\sqrt{50}-\sqrt{18}} = \frac{12\sqrt{3}}{"2"\sqrt{2}}$	Uses part (a) by replacing denominator by their $a\sqrt{2}$ where a is numeric. This is all that is required for this mark.	M1
	$= \frac{12\sqrt{3}}{2\sqrt{2}} = \frac{6\sqrt{3}}{\sqrt{2}} = \frac{\sqrt{108}}{\sqrt{2}} = \sqrt{54} = \sqrt{9}\sqrt{6}$	Cancels to obtain a multiple of $\sqrt{6}$. This is dependent on the first M1.	dM1
	$= 3\sqrt{6} \text{ Or } b=3, c=6$	Cao and cso	A1
			[3]
(b) WAY 4	$\frac{12\sqrt{3}}{\sqrt{50}-\sqrt{18}} = \frac{12\sqrt{3}}{"2"\sqrt{2}}$	Uses part (a) by replacing denominator by their $a\sqrt{2}$ where a is numeric. This is all that is required for this mark.	M1
	$\left(\frac{12\sqrt{3}}{2\sqrt{2}}\right)^2 = \frac{432}{8}$		
	$\sqrt{54} = \sqrt{9}\sqrt{6}$ $= 3\sqrt{6} \text{ Or } b=3, c=6$	Obtains a multiple of $\sqrt{6}$. This is dependent on the first M1.	dM1
		Cao and cso (do not allow $\pm 3\sqrt{6}$)	A1
			5 marks

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5.

Question Number	Scheme		Marks
1.(a)	20	Sight of 20. (4×5 is not sufficient)	B1
			(1)
(b)	$\frac{\sqrt{2}}{2\sqrt{5}-3\sqrt{2}} \times \frac{2\sqrt{5}+3\sqrt{2}}{2\sqrt{5}+3\sqrt{2}}$	Multiplies top and bottom by a correct expression. This statement is sufficient. NB $2\sqrt{5}+3\sqrt{2} \equiv \sqrt{20}+\sqrt{18}$	M1
		(Allow to multiply top and bottom by $k(2\sqrt{5}+3\sqrt{2})$)	
	$= \frac{\dots}{2}$	Obtains a denominator of 2 or sight of $(2\sqrt{5}-3\sqrt{2})(2\sqrt{5}+3\sqrt{2}) = 2$ with no errors seen in this expansion. May be implied by $\frac{\dots}{2k}$	A1
	Note that M0A1 is not possible. The 2 must come from a correct method.		
	Note that if M1 is scored there is no need to consider the numerator.		
	e.g. $\frac{2(MR?)}{2\sqrt{5}-3\sqrt{2}} \times \frac{2\sqrt{5}+3\sqrt{2}}{2\sqrt{5}+3\sqrt{2}} = \frac{\dots}{2}$ scores M1A1		

Numerator = $\sqrt{2}(2\sqrt{5} \pm 3\sqrt{2}) = 2\sqrt{10} \pm 6$	An attempt to multiply the numerator by $\pm(2\sqrt{5} \pm 3\sqrt{2})$ and obtain an expression of the form $p + q\sqrt{10}$ where p and q are integers. This may be implied by e.g. $2\sqrt{10} + 3\sqrt{4}$ or by their final answer.	M1
(Allow attempt to multiply the numerator by $k(2\sqrt{5} \pm 3\sqrt{2})$)		
$\frac{\sqrt{2}}{2\sqrt{5} - 3\sqrt{2}} = \frac{2\sqrt{10} + 6}{2} = 3 + \sqrt{10}$	Cso. For the answer as written or $\sqrt{10} + 3$ or a statement that $a = 3$ and $b = 10$. Score when first seen and ignore any subsequent attempt to 'simplify'. Allow $1\sqrt{10}$ for $\sqrt{10}$	A1
		(4)
		(5 marks)
Alternative for (b)		
$\frac{\sqrt{2}}{2\sqrt{5} - 3\sqrt{2}} = \frac{1}{\sqrt{10} - 3}$ or $\frac{2}{2\sqrt{10} - 6}$	M1: Divides or multiplies top and bottom by $\sqrt{2}$ A1: $\frac{k}{k(\sqrt{10} - 3)}$	M1A1
$= \frac{1}{\sqrt{10} - 3} \times \frac{\sqrt{10} + 3}{\sqrt{10} + 3}$	M1: Multiplies top and bottom by $\sqrt{10} + 3$	M1
$= 3 + \sqrt{10}$		A1

6.

Question Number	Scheme	Marks
7.(a)	$(4^x =)y^2$	Allow y^2 or $y \times y$ or "y squared" "4 ^x =" not required
Must be seen in part (a)		
		(1)
(b)	$8y^2 - 9y + 1 = (8y - 1)(y - 1) = 0 \Rightarrow y = \dots$ or $(8(2^x) - 1)((2^x) - 1) = 0 \Rightarrow 2^x = \dots$	For attempting to solve the given equation as a 3 term quadratic in y or as a 3 term quadratic in 2^x leading to a value of y or 2^x (Apply usual rules for solving the quadratic – see general guidance) Allow x (or any other letter) instead of y for this mark e.g. an attempt to solve $8x^2 - 9x + 1 = 0$
	$2^x \text{ (or } y) = \frac{1}{8}, 1$	Both correct answers of $\frac{1}{8}$ (oe) and 1 for 2^x or y or their letter but not x unless 2^x (or y) is implied later

$x = -3 \quad x = 0$	M1: A correct attempt to find one numerical value of x from their 2^x (or y) which must have come from a 3 term quadratic equation . If logs are used then they must be evaluated.	M1A1
	A1: Both $x = -3$ and/or $x = 0$ May be implied by e.g. $2^{-3} = \frac{1}{8}$ and $2^0 = 1$ and no extra values.	
		(4)
		(5 marks)

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7.

Question Number	Scheme	Marks
2.	(a) $32^{\frac{1}{5}} = 2$ (b) For 2^{-2} or $\frac{1}{4}$ or $\left(\frac{1}{2}\right)^2$ or 0.25 as coefficient of x^k , for any value of k including $k = 0$ Correct index for x so Ax^{-2} or $\frac{A}{x^2}$ o.e. for any value of A $= \frac{1}{4x^2}$ or $0.25x^{-2}$	B1 (1) M1 B1 A1 cao (3) 4 Marks

Notes

(a) B1 Answer 2 must be in part (a) for this mark

(b) Look at their final answer

M1 For 2^{-2} or $\frac{1}{4}$ or $\left(\frac{1}{2}\right)^2$ or 0.25 in their answer as coefficient of x^k for numerical value of k (including $k = 0$) so final answer $\frac{1}{4}$ is M1 B0 A0

B1 Ax^{-2} or $\frac{A}{x^2}$ or equivalent e.g. $Ax^{-\frac{10}{5}}$ or $Ax^{-\frac{50}{25}}$ i.e. correct power of x seen in final answer

May have a bracket provided it is $(Ax)^{-2}$ or $\left(\frac{A}{x}\right)^2$

A1 $\frac{1}{4x^2}$ or $\frac{1}{4}x^{-2}$ or $0.25x^{-2}$ oe but must be correct power **and** coefficient combined correctly and must not be followed by a different wrong answer.

Poor bracketing: $2x^{-2}$ earns M0 B1 A0 as correct power of x is seen in this solution (They can recover if they follow this with $\frac{1}{4x^2}$ etc)

Special case $(2x)^{-2}$ as a **final** answer and $\left(\frac{1}{2x}\right)^2$ can have M0 B1 A0 if the correct expanded answer is not seen

The correct answer $\frac{1}{4x^2}$ etc. followed by $\left(\frac{1}{2x}\right)^2$ or $(2x)^{-2}$, treat $\frac{1}{4x^2}$ as final answer so M1 B1 A1 isw

But the correct answer $\frac{1}{4x^2}$ etc clearly followed by the wrong $2x^{-2}$ or $4x^{-2}$, gets M1 B1 A0 do not ignore subsequent wrong work here

8.

Question Number	Scheme	Marks
6.	(a) $80 = 5 \times 16$ $\sqrt{80} = 4\sqrt{5}$	B1 (1)
	<div style="display: flex; justify-content: space-between;"> <div style="width: 45%;"> <p>Method 1</p> <p>(b) $\frac{\sqrt{80}}{\sqrt{5+1}}$ or $\frac{c\sqrt{5}}{\sqrt{5+1}}$</p> <p>$= \frac{\sqrt{80}}{\sqrt{5+1}} \times \frac{\sqrt{5-1}}{\sqrt{5-1}}$ or $\frac{\sqrt{80}}{1+\sqrt{5}} \times \frac{1-\sqrt{5}}{1-\sqrt{5}}$</p> <p>$= \frac{20-4\sqrt{5}}{4}$ or $\frac{4\sqrt{5}-20}{-4}$</p> <p>$= 5-\sqrt{5}$</p> </div> <div style="width: 45%; border-left: 1px solid black; padding-left: 10px;"> <p>Method 2</p> <p>$(p+q\sqrt{5})(\sqrt{5}+1)=\sqrt{80}$</p> <p>$p\sqrt{5}+q\sqrt{5}+p+5q = 4\sqrt{5}$</p> <p>$p+5q=0$ $p+q=4$ $p=5, q=-1$</p> </div> </div>	B1ft M1 A1 A1cao (4) (5 marks)

Notes

(a) B1 Accept $4\sqrt{5}$ or $c=4$ – no working necessary

(b)
(Method 1)

B1ft Only ft on c See $\frac{\sqrt{80}}{\sqrt{5+1}}$ or $\frac{c\sqrt{5}}{\sqrt{5+1}}$

M1 State intention to multiply by $\sqrt{5-1}$ or $1-\sqrt{5}$ in the numerator **and** the denominator

A1 Obtain denominator of 4 (for $\sqrt{5-1}$) or -4 (for $1-\sqrt{5}$) **or** correct simplified numerator of $20-4\sqrt{5}$ or $4(5-\sqrt{5})$ **or** $4\sqrt{5}-20$ or $4(\sqrt{5}-5)$ **So either numerator or denominator must be correct**

A1 Correct answer only. Both **numerator and denominator must have been correct and division of numerator and denominator by 4 has been performed.**

Accept $p=5, q=-1$ or accept $5-\sqrt{5}$ or $-\sqrt{5}+5$ Also accept $5-1\sqrt{5}$

(Method 2)

B1ft Only fit on c $(p+q\sqrt{5})(\sqrt{5}+1)=\sqrt{80}$ or $c\sqrt{5}$

M1 Multiply out the lhs and replace $\sqrt{80}$ by $c\sqrt{5}$

A1 Compare rational and irrational parts to give $p + q = 4$, and $p + 5q = 0$

A1 Solve equations to give $p = 5$, $q = -1$

Common error:

$\frac{\sqrt{80}}{1+\sqrt{5}} \times \frac{1-\sqrt{5}}{1-\sqrt{5}} = \frac{4\sqrt{5}-20}{4} = \sqrt{5}-5$ gets B1 M1 A1 (for correct numerator – denominator is wrong for their product) then A0

Correct answer with no working – send to review – have they used a calculator?

Correct answer after trial and improvement with evidence that $(5-\sqrt{5})(\sqrt{5}+1)=\sqrt{80}$ could earn all four marks

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9.

Question Number	Scheme		Marks
1	$\frac{7+\sqrt{5}}{\sqrt{5}-1} \times \frac{(\sqrt{5}+1)}{(\sqrt{5}+1)}$	Multiplies top and bottom by a correct expression. This statement is sufficient.	M1
	(Allow to multiply top and bottom by $k(\sqrt{5}+1)$)		
	$= \frac{\dots}{4}$	Obtains a denominator of 4 or sight of $(\sqrt{5}-1)(\sqrt{5}+1)=4$	A1cso
	Note that M0A1 is not possible. The 4 must come from a correct method.		
	$(7+\sqrt{5})(\sqrt{5}+1) = 7\sqrt{5} + 5 + 7 + \sqrt{5}$	An attempt to multiply the numerator by $(\pm\sqrt{5} \pm 1)$ and get 4 terms with at least 2 correct for their $(\pm\sqrt{5} \pm 1)$. (May be implied)	M1
	$3 + 2\sqrt{5}$	Answer as written or $a = 3$ and $b = 2$. (Allow $2\sqrt{5} + 3$)	A1cso
	Correct answer with no working scores full marks		
			[4]

Way 2	$\frac{7+\sqrt{5}}{\sqrt{5}-1} \times \frac{(-\sqrt{5}-1)}{(-\sqrt{5}-1)}$	Multiplies top and bottom by a correct expression. This statement is sufficient.	M1
	(Allow to multiply top and bottom by $k(-\sqrt{5}-1)$)		
	$= \frac{\dots}{-4}$	Obtains a denominator of -4	A1cso
	$(7+\sqrt{5})(-\sqrt{5}-1) = -7\sqrt{5} - 5 - 7 - \sqrt{5}$	An attempt to multiply the numerator by $(\pm\sqrt{5} \pm 1)$ and get 4 terms with at least 2 correct for their $(\pm\sqrt{5} \pm 1)$. (May be implied)	M1
	$3 + 2\sqrt{5}$	Answer as written or $a = 3$ and $b = 2$	A1cso
	Correct answer with no working scores full marks		
			[4]
	<p>Alternative using Simultaneous Equations:</p> $\frac{(7+\sqrt{5})}{\sqrt{5}-1} = a + b\sqrt{5} \Rightarrow 7 + \sqrt{5} = (a-b)\sqrt{5} + 5b - a$ <p>M1 Multiplies and collects rational and irrational parts $a - b = 1, 5b - a = 7$ A1 Correct equations $a = 3, b = 2$ M1 for attempt to solve simultaneous equations A1 both answers correct</p>		

10.

Question Number	Scheme		Marks
3(a)	$8^{\frac{1}{3}} = 2$ or $8^5 = 32768$	A correct attempt to deal with the $\frac{1}{3}$ or the 5. $8^{\frac{1}{3}} = \sqrt[3]{8}$ or $8^5 = 8 \times 8 \times 8 \times 8 \times 8$	M1
	$\left(8^{\frac{5}{3}} = \right) 32$	Cao	A1
	A correct answer with no working scores full marks		
	<p>Alternative</p> $8^{\frac{5}{3}} = 8 \times 8^{\frac{2}{3}} = 8 \times 2^2 = 32$ <p>M1 (Deals with the 1/3) = 32 A1</p>		
			(2)

(b)	$\left(2x^{\frac{1}{2}}\right)^3 = 2^3 x^{\frac{3}{2}}$	One correct power either 2^3 or $x^{\frac{3}{2}}$. $\left(2x^{\frac{1}{2}}\right) \times \left(2x^{\frac{1}{2}}\right) \times \left(2x^{\frac{1}{2}}\right)$ on its own is not sufficient for this mark.	M1
	$\frac{8x^{\frac{3}{2}}}{4x^2} = 2x^{-\frac{1}{2}} \text{ or } \frac{2}{\sqrt{x}}$	M1: Divides coefficients of x and subtracts their powers of x . Dependent on the previous M1	dM1A1
		A1: Correct answer	
	Note that unless the power of x implies that they have subtracted their powers you would need to see evidence of subtraction. E.g. $\frac{8x^{\frac{3}{2}}}{4x^2} = 2x^{\frac{3}{2}}$ would score dM0 unless you see some evidence that $3/2 - 2$ was intended for the power of x .		
	Note that there is a misconception that $\frac{\left(2x^{\frac{1}{2}}\right)^3}{4x^2} = \left(\frac{2x^{\frac{1}{2}}}{4x^2}\right)^3$ - this scores 0/3		
			(3)
			(5)

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11.

Question Number	Scheme	Marks
2.	$(8^{2x+3} = (2^3)^{2x+3}) = 2^{3(2x+3)} \text{ or } 2^{ax+b} \text{ with } a = 6 \text{ or } b = 9$ $= 2^{6x+9} \text{ or } 2^{3(2x+3)} \text{ as final answer with no errors or } (y=)6x+9 \text{ or } 3(2x+3)$	M1 A1 [2]
	Notes	2 marks
	M1: Uses $8 = 2^3$, and multiplies powers $3(2x+3)$. Does not add powers. (Just $8 = 2^3$ or $8^{\frac{1}{2}} = 2$ is M0) A1: Either 2^{6x+9} or $2^{3(2x+3)}$ or $(y=)6x+9$ or $3(2x+3)$	
	Note: Examples: 2^{6x+9} scores M1A0 $: 8^{2x+3} = (2^3)^{2x+3} = 2^{3+2x+3}$ gets M0A0 Special case: $: = 2^{6x} 2^9$ without seeing as single power M1A0 Alternative method using logs: $8^{2x+3} = 2^y \Rightarrow (2x+3)\log 8 = y \log 2 \Rightarrow y = \frac{(2x+3)\log 8}{\log 2}$ So $(y=)6x+9$ or $3(2x+3)$	M1 A1 [2]

12.

Question Number	Scheme			Marks
3. (i)	$(5 - \sqrt{8})(1 + \sqrt{2})$ $= 5 + 5\sqrt{2} - \sqrt{8} - 4$ $= 5 + 5\sqrt{2} - 2\sqrt{2} - 4$ $= 1 + 3\sqrt{2}$			M1 B1 A1 [3]
(ii)	Method 1 Either $\sqrt{80} + \frac{30}{\sqrt{5}} \left(\frac{\sqrt{5}}{\sqrt{5}} \right)$ $= 4\sqrt{5} + \dots$ $= 4\sqrt{5} + 6\sqrt{5}$	Method 2 Or $\left(\frac{\sqrt{400} + 30}{\sqrt{5}} \right) \frac{\sqrt{5}}{\sqrt{5}}$ $= \left(\frac{20 + \dots}{\dots} \right) \dots$ $= \left(\frac{50\sqrt{5}}{5} \right)$ $= 10\sqrt{5}$	Method 3 $\sqrt{80} + \frac{\sqrt{900}}{\sqrt{5}} = \sqrt{80} + \sqrt{180}$ $= 4\sqrt{5} + \dots$ $= 4\sqrt{5} + 6\sqrt{5}$	M1 B1 A1 [3]
Alternative for (i)	$(5 - 2\sqrt{2})(1 + \sqrt{2})$ $= 5 + 5\sqrt{2} - 2\sqrt{2} - 2\sqrt{2}\sqrt{2}$ $= 1 + 3\sqrt{2}$			This earns the B1 mark and is entered on open as B1 Multiplies out correctly with $2\sqrt{2}$. This may be seen or implied and may be simplified e.g. $= 5 + 3\sqrt{2} - 2\sqrt{4}$ o.e. For earlier use of $2\sqrt{2}$ $1 + 3\sqrt{2}$ or $a = 1$ and $b = 3$. M1 B1 A1 [3] 6 marks
Notes				
(i)	M1: Multiplies out brackets correctly giving four correct terms or simplifying to correct expansion. (This may be implied by correct answer) – can appear as table B1: $\sqrt{8} = 2\sqrt{2}$, seen or implied at any point A1: Fully and correctly simplified to $1 + 3\sqrt{2}$ or $a = 1$ and $b = 3$.			
(ii)	M1: Rationalises denominator i.e. Multiplies $\left(\frac{k}{\sqrt{5}} \right)$ by $\left(\frac{\sqrt{5}}{\sqrt{5}} \right)$ or $\left(\frac{-\sqrt{5}}{-\sqrt{5}} \right)$, seen or implied or uses Method 3 or similar e.g. $\left(\frac{30}{\sqrt{5}} \right) = \frac{6 \times 5}{\sqrt{5}} = 6\sqrt{5}$ B1: (Independent mark) States $\sqrt{80} = 4\sqrt{5}$ Or either $\sqrt{400} = 20$ or $\sqrt{80}\sqrt{5} = 20$ at any point if they use Method 2. A1: $10\sqrt{5}$ or $c = 10$.			
N.B There are other methods e.g. $\sqrt{80} = \frac{20}{\sqrt{5}}$ (B1) then add $\frac{20}{\sqrt{5}} + \frac{30}{\sqrt{5}} = \frac{50}{\sqrt{5}}$ then M1 A1 as before Those who multiply initial expression by $\sqrt{5}$ to obtain $\sqrt{400} + 30 = 20 + 30 = 50$ earn M0 B1 A0				

13.

Question Number	Scheme	Marks
2. (a)	$\left\{ (32)^{\frac{3}{5}} \right\} = \left(\sqrt[5]{32} \right)^3 \text{ or } \sqrt[5]{(32)^3} \text{ or } 2^3 \text{ or } \sqrt[5]{32768}$ $= 8$	M1 A1 [2]
(b)	$\left\{ \left(\frac{25x^4}{4} \right)^{-\frac{1}{2}} \right\} = \left(\frac{4}{25x^4} \right)^{\frac{1}{2}} \text{ or } \left(\frac{5x^2}{2} \right)^{-1} \text{ or } \frac{1}{\left(\frac{25x^4}{4} \right)^{\frac{1}{2}}}$ $= \frac{2}{5x^2} \text{ or } \frac{2}{5}x^{-2}$	See notes below M1
Notes		
(a)	<p>M1: for a full correct interpretation of the fractional power. Note: $5 \times (32)^3$ is M0. A1: for 8 only. Note: Award M1A1 for writing down 8.</p>	
(b)	<p>M1: For use of $\frac{1}{2}$ OR use of -1</p> <p>Use of $\frac{1}{2}$: Candidate needs to demonstrate they have rooted all three elements in their bracket.</p> <p>Use of -1: Either Candidate has $\frac{1}{\text{Bracket}}$ or $\left(\frac{Ax^C}{B} \right)$ becomes $\left(\frac{B}{Ax^C} \right)$.</p> <p>Allow M1 for...</p> <ul style="list-style-type: none"> • $\left(\frac{4}{25x^4} \right)^{\frac{1}{2}}$ or $\left(\frac{5x^2}{2} \right)^{-1}$ or $\frac{1}{\left(\frac{25x^4}{4} \right)^{\frac{1}{2}}}$ or $\sqrt{\left(\frac{4}{25x^4} \right)}$ or $\frac{1}{\sqrt{\left(\frac{25x^4}{4} \right)}}$ or $\left(\frac{1}{\frac{25x^4}{4}} \right)^{\frac{1}{2}}$ or $\frac{1}{\frac{5x^2}{2}}$ or $\frac{1}{\frac{1}{2}}$ or $\frac{1}{\frac{1}{2}}$ or $-\left(\frac{5x^2}{2} \right)$ or $\left(\frac{-5x^2}{-2} \right)$ or $-\left(\frac{5x^2}{2} \right)$ or $\frac{5x^2}{2}$ • $\left(\frac{4}{25x^4} \right)^K$ or $\left(\frac{5x^2}{2} \right)^C$ where K, C are any powers including 1. <p>A1: for either $\frac{2}{5x^2}$ or $\frac{2}{5}x^{-2}$ or $0.4x^{-2}$ or $\frac{0.4}{x^2}$.</p> <p>Note: $\left(\sqrt{\left(\frac{25x^4}{4} \right)} \right)^{-1}$ is not enough work by itself for the method mark.</p> <p>Note: A final answer of $\frac{1}{\frac{5}{2}x^2}$ or $\frac{1}{2\frac{1}{2}x^2}$ or $\frac{1}{2.5x^2}$ is A0.</p> <p>Note: Also allow $\pm \frac{2}{5x^2}$ or $\pm \frac{2}{5}x^{-2}$ or $\pm 0.4x^{-2}$ or $\pm \frac{0.4}{x^2}$ for A1.</p>	

14.

Question Number	Scheme	Marks
3.	$\left\{ \frac{2}{\sqrt{12} - \sqrt{8}} \right\} = \frac{2}{(\sqrt{12} - \sqrt{8})} \times \frac{(\sqrt{12} + \sqrt{8})}{(\sqrt{12} + \sqrt{8})}$ $= \frac{\{2(\sqrt{12} + \sqrt{8})\}}{12 - 8}$ $= \frac{2(2\sqrt{3} + 2\sqrt{2})}{12 - 8}$ $= \sqrt{3} + \sqrt{2}$	<p>Writing this is sufficient for M1.</p> <p>For 12 – 8. This mark can be implied.</p> <p>M1 A1 B1 B1 A1 cs0</p> <p style="text-align: right;">5</p>
Notes		
<p>MI: for a correct method to rationalise the denominator.</p> <p>1st A1: $(\sqrt{12} - \sqrt{8})(\sqrt{12} + \sqrt{8}) \rightarrow 12 - 8$ or $(\sqrt{3} + \sqrt{2})(\sqrt{3} - \sqrt{2}) \rightarrow 3 - 2$</p> <p>1st B1: for $\sqrt{12} = 2\sqrt{3}$ or $\sqrt{48} = 4\sqrt{3}$ seen or implied in candidate's working.</p> <p>2nd B1: for $\sqrt{8} = 2\sqrt{2}$ or $\sqrt{32} = 4\sqrt{2}$ seen or implied in candidate's working.</p> <p>2nd A1: for $\sqrt{3} + \sqrt{2}$. Note: $\frac{\sqrt{3} + \sqrt{2}}{1}$ as a final answer is A0.</p> <p>Note: The first accuracy mark is dependent on the first method mark being awarded.</p> <p>Note: $\frac{1}{2}\sqrt{12} + \frac{1}{2}\sqrt{8} = \sqrt{3} + \sqrt{2}$ with no intermediate working implies the B1B1 marks.</p> <p>Note: $\sqrt{12} = \sqrt{4}\sqrt{3}$ or $\sqrt{8} = \sqrt{4}\sqrt{2}$ are not sufficient for the B1 marks.</p> <p>Note: A candidate who writes down (by misread) $\sqrt{18}$ for $\sqrt{8}$ can potentially obtain M1A0B1B1A0, where the 2nd B1 will be awarded for $\sqrt{18} = 3\sqrt{2}$ or $\sqrt{72} = 6\sqrt{2}$</p> <p>Note: The final accuracy mark is for a correct solution only.</p>		
<p><u>Alternative 1 solution</u></p> $\left\{ \frac{2}{\sqrt{12} - \sqrt{8}} \right\} = \frac{2}{(2\sqrt{3} - 2\sqrt{2})} \quad \text{B1 B1}$ $= \frac{1}{(\sqrt{3} - \sqrt{2})} \times \frac{(\sqrt{3} + \sqrt{2})}{(\sqrt{3} + \sqrt{2})} \quad \text{M1}$ $= \frac{\{(\sqrt{3} + \sqrt{2})\}}{3 - 2} \quad \text{A1 for 3 - 2}$ $= \sqrt{3} + \sqrt{2} \quad \text{A1}$		
<p><u>Alternative 2 solution</u></p> $\left\{ \frac{2}{\sqrt{12} - \sqrt{8}} \right\} = \frac{2}{(2\sqrt{3} - 2\sqrt{2})} = \frac{1}{(\sqrt{3} - \sqrt{2})} = \sqrt{3} + \sqrt{2}, \quad \text{or} \quad \frac{2}{(2\sqrt{3} - 2\sqrt{2})} = \sqrt{3} + \sqrt{2}$ <p>with no incorrect working seen is awarded M1A1B1B1A1.</p> <div style="border: 1px solid black; padding: 10px; width: fit-content; margin-left: auto; margin-right: auto;"> <p>Please record the marks in the relevant places on the mark grid.</p> </div>		

15.

Question	Scheme	Marks
<p>2. (a)</p> <p>(b)</p>	$\sqrt{32} = 4\sqrt{2} \text{ or } \sqrt{18} = 3\sqrt{2}$ $(\sqrt{32} + \sqrt{18}) = \underline{7\sqrt{2}}$ <p>or</p> $\times \frac{3-\sqrt{2}}{3-\sqrt{2}} \text{ or } \times \frac{-3+\sqrt{2}}{-3+\sqrt{2}} \text{ seen}$ $\left[\frac{\sqrt{32} + \sqrt{18}}{3+\sqrt{2}} \times \frac{3-\sqrt{2}}{3-\sqrt{2}} \right] = \frac{a\sqrt{2}(3-\sqrt{2})}{[9-2]} \rightarrow \frac{3a\sqrt{2}-2a}{[9-2]} \text{ (or better)}$ $= \underline{3\sqrt{2}, -2}$	<p>B1</p> <p>B1 (2)</p> <p>M1</p> <p>dM1</p> <p>A1, A1 (4)</p>
<p>ALT</p>	<p>$(b\sqrt{2} + c)(3 + \sqrt{2}) = 7\sqrt{2}$ leading to: $3b + c = 7, \quad 3c + 2b = 0$</p> <p>e.g. $3(7 - 3b) + 2b = 0$ (o.e.)</p>	<p>M1</p> <p>dM1</p>
6 marks		
Notes		
<p>(a)</p> <p>(b)</p> <p>ALT</p>	<p>1st B1 for either surd simplified</p> <p>2nd B1 for $7\sqrt{2}$ or accept $a = 7$. Answer only scores B1B1</p> <p>NB Common error is $\sqrt{32} + \sqrt{18} = \sqrt{50} = 5\sqrt{2}$ this scores B0B0 but can use their "5" in (b) to get M1M1</p> <p>1st M1 for an attempt to multiply by $\frac{3-\sqrt{2}}{3-\sqrt{2}}$ (o.e.) Allow poor use of brackets</p> <p>2nd dM1 for using $a\sqrt{2}$ to correctly obtain a numerator of the form $p + q\sqrt{2}$ where p and q are non-zero integers. Allow arithmetic slips e.g. $21\sqrt{2} - 28$ or $3\sqrt{2} \times \sqrt{2} = 3$</p> <p>Follow through their $a = 7$ or a new value found in (b). Ignore denominator.</p> <p>Allow use of letter a. Dependent on 1st M1</p> <p>So $3\sqrt{32} - \sqrt{64} + 3\sqrt{8} - \sqrt{36}$ is M0 until they reduce $p + q\sqrt{2}$</p> <p>1st A1 for $3\sqrt{2}$ or accept $b = 3$ from correct working</p> <p>2nd A1 for -2 or accept $c = -2$ from correct working</p> <p>Simultaneous Equations</p> <p>1st M1 for $(b\sqrt{2} + c)(3 + \sqrt{2}) = 7\sqrt{2}$ and forming 2 simultaneous equations. Ft their $a = 7$</p> <p>2nd dM1 for solving their simultaneous equations: reducing to a linear equation in one variable</p>	

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16.

Question Number	Scheme	Marks
1. (a)	5 (or ± 5)	B1 (1)
(b)	$25^{\frac{3}{2}} = \frac{1}{25^{\frac{3}{2}}}$ or $25^{\frac{3}{2}} = 125$ or better $\frac{1}{125}$ or 0.008 (or $\pm \frac{1}{125}$)	M1 A1 (2) 3
Notes		
(a) Give B1 for 5 or ± 5 Anything else is B0 (including just -5) (b) M: Requires reciprocal OR $25^{\frac{3}{2}} = 125$ Accept $\frac{1}{5^3}, \frac{1}{\sqrt{15625}}, \frac{1}{25 \times 5}, \frac{1}{25\sqrt{25}}, \frac{1}{\sqrt{25^3}}$ for M1 Correct answer with no working (or notation errors in working) scores both marks i.e. M1 A1 M1A0 for $-\frac{1}{125}$ without $+\frac{1}{125}$		

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17.

Question Number	Scheme	Marks
1. (a)	$16^{\frac{1}{4}} = 2$ or $\frac{1}{16^{\frac{1}{4}}}$ or better $\left(16^{-\frac{1}{4}} = \right) \frac{1}{2}$ or 0.5 (ignore \pm)	M1 A1 (2)
(b)	$\left(2x^{-\frac{1}{4}}\right)^4 = 2^4 x^{-4}$ or $\frac{2^4}{x^4}$ or equivalent $x\left(2x^{-\frac{1}{4}}\right)^4 = 2^4$ or 16	M1 A1 cao (2) 4

<u>Notes</u>	
(a)	M1 for a correct statement dealing with the $\frac{1}{4}$ or the $-$ power This may be awarded if 2 is seen or for reciprocal of their $16^{\frac{1}{4}}$ s.c. $\frac{1}{4}$ is M1 A0, also 2^{-1} is M1 A0 $\pm\frac{1}{2}$ is not penalised so M1 A1
(b)	M1 for correct use of the power 4 on both the 2 and the x terms A1 for cancelling the x and simplifying to one of these two forms. Correct answers with no working get full marks

18.

Question Number	Scheme	Marks
3.	$\frac{5-2\sqrt{3}}{\sqrt{3}-1} \times \frac{(\sqrt{3}+1)}{(\sqrt{3}+1)}$ $= \frac{\dots}{2} \quad \text{denominator of 2}$ Numerator = $5\sqrt{3} + 5 - 2\sqrt{3}\sqrt{3} - 2\sqrt{3}$ So $\frac{5-2\sqrt{3}}{\sqrt{3}-1} = -\frac{1}{2} + \frac{3}{2}\sqrt{3}$	M1 A1 M1 A1 4
	Alternative: $(p+q\sqrt{3})(\sqrt{3}-1) = 5-2\sqrt{3}$, and form simultaneous equations in p and q $-p+3q=5$ and $p-q=-2$ Solve simultaneous equations to give $p = -\frac{1}{2}$ and $q = \frac{3}{2}$.	M1 A1 M1 A1
<u>Notes</u>		
	1 st M1 for multiplying numerator and denominator by same correct expression 1 st A1 for a correct denominator as a single number (NB depends on M mark) 2 nd M1 for an attempt to multiply the numerator by $(\sqrt{3} \pm 1)$ and get 4 terms with at least 2 correct. 2 nd A1 for the answer as written or $p = -\frac{1}{2}$ and $q = \frac{3}{2}$. Allow -0.5 and 1.5 . (Apply isw if correct answer seen, then slip writing $p = , q =$)	
	Answer only (very unlikely) is full marks if correct – no part marks	

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19.

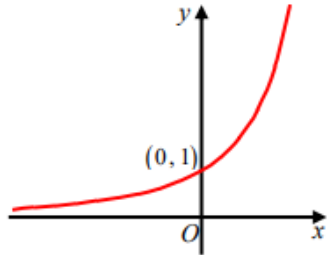
Question Number	Scheme	Marks
1.	$(\sqrt{75} - \sqrt{27}) = 5\sqrt{3} - 3\sqrt{3}$ $= 2\sqrt{3}$	M1 A1 2
	<u>Notes</u>	
	<p>M1 for $5\sqrt{3}$ from $\sqrt{75}$ or $3\sqrt{3}$ from $\sqrt{27}$ seen anywhere</p> <p>A1 for $2\sqrt{3}$; allow $\sqrt{12}$ or $k = 2, x = 3$ allow $k = 1, x = 12$</p> <p><u>Some Common errors</u></p> <p>$\sqrt{75} - \sqrt{27} = \sqrt{48}$ leading to $4\sqrt{3}$ is M0A0</p> <p>$25\sqrt{3} - 9\sqrt{3} = 16\sqrt{3}$ is M0A0</p>	

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20.

Question number	Scheme	Marks
Q2	<p>(a) $(7 + \sqrt{5})(3 - \sqrt{5}) = 21 - 5 + 3\sqrt{5} - 7\sqrt{5}$ Expand to get 3 or 4 terms</p> $= 16, -4\sqrt{5}$ (1 st A for 16, 2 nd A for $-4\sqrt{5}$) (i.s.w. if necessary, e.g. $16 - 4\sqrt{5} \rightarrow 4 - \sqrt{5}$)	M1 A1, A1 (3)
	<p>(b) $\frac{7 + \sqrt{5}}{3 + \sqrt{5}} \times \frac{3 - \sqrt{5}}{3 - \sqrt{5}}$ (This is sufficient for the M mark)</p> <p>Correct denominator without surds, i.e. $9 - 5$ or 4</p> $4 - \sqrt{5}$ or $4 - 1\sqrt{5}$	M1 A1 A1 (3) [6]

	<p>(a) M1: Allowed for an attempt giving 3 or 4 terms, with at least 2 correct (even if unsimplified). e.g. $21 - \sqrt{5^2} + \sqrt{15}$ scores M1. Answer only: $16 - 4\sqrt{5}$ scores full marks One term correct scores the M mark by implication, e.g. $26 - 4\sqrt{5}$ scores M1 A0 A1</p> <p>(b) Answer only: $4 - \sqrt{5}$ scores full marks One term correct scores the M mark by implication, e.g. $4 + \sqrt{5}$ scores M1 A0 A0 $16 - \sqrt{5}$ scores M1 A0 A0</p> <p>Ignore subsequent working, e.g. $4 - \sqrt{5}$ so $a = 4, b = 1$</p> <p>Note that, as always, A marks are dependent upon the preceding M mark, so that, for example, $\frac{7 + \sqrt{5}}{3 + \sqrt{5}} \times \frac{3 + \sqrt{5}}{3 - \sqrt{5}} = \frac{\dots\dots}{4}$ is M0 A0.</p> <p><u>Alternative</u></p> <p>$(a + b\sqrt{5})(3 + \sqrt{5}) = 7 + \sqrt{5}$, then form simultaneous equations in a and b. M1</p> <p>Correct equations: $3a + 5b = 7$ and $3b + a = 1$ A1 $a = 4$ and $b = -1$ A1</p>	
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Question Number	Scheme	Marks
<p>8.</p> <p>(a)</p>	<p>Graph of $y = 7^x, x \in \mathbb{R}$ and solving $7^{2x} - 4(7^x) + 3 = 0$</p>  <p>At least two of the three criteria correct. (See notes below.)</p> <p>All three criteria correct. (See notes below.)</p>	<p>B1</p> <p>B1</p> <p>(2)</p>
<p>(b)</p>	<p>$y^2 - 4y + 3 = 0$</p> <p>$\{(y-3)(y-1) = 0 \text{ or } (7^x - 3)(7^x - 1) = 0\}$</p> <p>$y = 3, y = 1 \text{ or } 7^x = 3, 7^x = 1$</p> <p>$\{7^x = 3 \Rightarrow\} x \log 7 = \log 3$</p> <p>or $x = \frac{\log 3}{\log 7}$ or $x = \log_7 3$</p> <p>$x = 0.5645\dots$</p> <p>$x = 0$</p>	<p>Forming a quadratic {using "y" = 7^x}. M1</p> <p>$y^2 - 4y + 3 = 0$ A1</p> <p>Both $y = 3$ and $y = 1$. A1</p> <p>A valid method for solving $7^x = k$ where $k > 0, k \neq 1$ dM1</p> <p>0.565 or awrt 0.56 A1</p> <p>$x = 0$ stated as a solution. B1</p> <p>(6)</p> <p>[8]</p>
Notes		
<p>(a)</p>	<p>B1B0: Any two of the following three criteria below correct. B1B1: All three criteria correct. Criteria number 1: Correct shape of curve for $x \geq 0$. Criteria number 2: Correct shape of curve for $x < 0$. Criteria number 3: (0, 1) stated or 1 marked on the y-axis. Allow (1, 0) rather than (0, 1) if marked in the "correct" place on the y-axis.</p>	
<p>(b)</p>	<p>1st M1 is an attempt to form a quadratic equation {using "y" = 7^x.}</p> <p>1st A1 mark is for the correct quadratic equation of $y^2 - 4y + 3 = 0$.</p> <p>Can use any variable here, eg: y, x or 7^x. Allow M1A1 for $x^2 - 4x + 3 = 0$.</p> <p>Writing $(7^x)^2 - 4(7^x) + 3 = 0$ is also sufficient for M1A1.</p> <p>Award M0A0 for seeing $7^{2x} - 4(7^x) + 3 = 0$ by itself without seeing $y^2 - 4y + 3 = 0$ or $(7^x)^2 - 4(7^x) + 3 = 0$.</p> <p>1st A1 mark for both $y = 3$ and $y = 1$ or both $7^x = 3$ and $7^x = 1$. Do not give this accuracy mark for both $x = 3$ and $x = 1$, unless these are recovered in later working by candidate applying logarithms on these.</p> <p>Award M1A1A1 for $7^x = 3$ and $7^x = 1$ written down with no earlier working.</p> <p>3rd dM1 for solving $7^x = k, k > 0, k \neq 1$ to give either $x \ln 7 = \ln k$ or $x = \frac{\ln k}{\ln 7}$ or $x = \log_7 k$.</p> <p>dM1 is dependent upon the award of M1.</p> <p>2nd A1 for 0.565 or awrt 0.56. B1 is for the solution of $x = 0$, from <i>any</i> working.</p>	

